

## Exercise 7.1

## Question

7.1. *Engulf and Devour*

The safety engineer for Engulf and Devour's Lakeside factory has estimated the number of employee disabilities (measured in sick days/year) that can be avoided by various measures: covering dangerous machinery (CDM), providing protective clothing (PPC), improving ventilation (IV), and/or lowering noise levels (LNL). The information is summarized in the following table.

Investment (10 <sup>3</sup> \$)	Measures			
	CDM	PPC	IV	LNL
0	0	0	0	0
10	5	15	2	5
20	10	22	12	7
30	15	25	15	15
40	20	25	17	25
50	22	30	25	26

- Use dynamic programming to determine how a \$70,000 budget could be most effectively employed to reduce disabilities.
- How much of a difference would it make if management cut back the safety budget to \$60,000? How much money would be saved for each additional sick day the budget cut would cause?
- Could this problem be solved by linear programming? Why or why not?

**Solution from Manual**

Chapter 7

7.1 Engulf and Devour

a) Best investment gives a savings of 52 days via two possible investment schemes: (0,10,20,40) or (10,20,0,40). See Table:

Budget \$000	$f_1(K)$	$f_2(K)$	$f_3(K)$	$f_4(K)$
0	0	0	0	0
10	5	15	15	
20	10	22	22	
30	15	27	27	
40	20	32	34	
50	22	37	39	
60	22	42	44	47
70	22	45	49	52

b) Five less days would be saved ( $52 - 47 = 5$ ) at a savings of \$10,000 which is \$2,000 per sick day.

c) This problem could not be solved by LP since the return functions for PPC, IV, Z LNL all present non-convex feasible regions.

Additional Notes

7.1.

Budget	$f_1(k)$	$f_2(k)$	$f_3(k)$	$f_4(k)$
0	0	0	$\emptyset$	$\emptyset$
10	5	15 (0,10)	15 (0,10,0)	
20	10	22 (0,20)	22 (0,20,0)	
30	15	27 (0,20)	27 (0,20,0)	
40	20	32 (20,20)	34 (0,20,20)	
50	22	37 (30,20)	38 (10,20,20)	
60	22	42 (40,20)	44 (20,20,20)	47 (0,20,0,40)
70	22	45 (40,30)	49 (30,20,20)	52 (10,20,0,40); (0,10,20,10)

$f_1(k) = \max\{0, k_i + f_{i-1}(k - x_i)\}$

(a) 70k:  $f(k) = 52$   
 (b) 60k:  $f(0,20,0,40) = 47$   
 $\Delta \text{ budget} = 10k$   
 $\Delta \text{ sick days} = 52 - 47 = 5 \text{ days}$   
 $\Downarrow$   
 $\$2k / \text{sick day}$   
 (c) NO!  
 Return  $f$ 's are non-linear  
 $\Rightarrow$  non-convex feasible region.